Contents

Index of Notation xvi

1 • Introduction 1
  1.1 Objectives of Diagnostic Measurement  2
  1.2 Diagnostic Measurement with DCMs  3
  1.3 Selecting versus Constructing DCMs  3
  1.4 The Role of DCMs in Diagnostic Assessment Design and Implementation  4

I. THEORY: PRINCIPLES OF DIAGNOSTIC MEASUREMENT WITH DCMs

2 • Implementation, Design, and Validation of Diagnostic Assessments 9
  2.1 Diagnostic Assessment in Education 10
  2.2 The Process Character of Diagnostic Assessment Implementations 10
  2.3 Frameworks for Principled Design of Diagnostic Assessments 15
  2.4 Frameworks for Validity Studies of Diagnostic Assessments 25
  2.5 Chapter Conclusion 28

3 • Diagnostic Decision Making with DCMs 29
  3.1 Diagnostic Characteristics of DCMs 29
  3.2 Developing Diagnostic Rules 32
  3.3 Contexts for Using DCMs 40
  3.4 Reduction of Classification Error with DCMs 45
  3.5 Chapter Conclusion 47

4 • Attribute Specification for DCMs 49
  4.1 The Nature of Attributes 49
  4.2 Attribute Hierarchies 55
  4.3 Reporting Attribute Profiles 64
  4.4 Developing Cognitive Processing Models 71
  4.5 Chapter Conclusion 77
# II. METHODS: PSYCHOMETRIC FOUNDATIONS OF DCMs

## 5 • The Statistical Nature of DCMs

- 5.1 DCMs and Other Latent-Variable Models 81
- 5.2 A Taxonomy of Core DCMs 96
- 5.3 Related Classification Approaches 101
- 5.4 Bayesian Inference Networks 108
- 5.5 Chapter Conclusion 111

## 6 • The Statistical Structure of Core DCMs

- 6.1 General Mathematical Structure of DCMs 113
- 6.2 Noncompensatory DCMs 115
- 6.3 Compensatory DCMs 130
- 6.4 Chapter Conclusion 143

## 7 • The LCDM Framework

- 7.1 A Brief Introduction to Log-Linear Models 145
- 7.2 Log-Linear Models with Latent Classes 148
- 7.3 Representing DCMs as Log-Linear Models with Latent Classes 150
- 7.4 The LCDM as a General DCM for Diagnostic Measurement 155
- 7.5 Representing Core DCMs with the LCDM 158
- 7.6 Chapter Conclusion 168

## 8 • Modeling the Attribute Space in DCMs

- 8.1 Structural Models in DCMs 169
- 8.2 Unstructured Structural Models 171
- 8.3 Log-Linear Structural Models 175
- 8.4 Unstructured Tetrachoric Models 178
- 8.5 Structured Tetrachoric Models 182
- 8.6 Summary of Parameter Complexity in Structural Models 187
- 8.7 Special Topics for Structural Models 188
- 8.8 Chapter Conclusion 190

# III. APPLICATIONS: UTILIZING DCMs IN PRACTICE

## 9 • Estimating DCMs Using Mplus

- 9.1 Sample Data Set 194
- 9.2 Basic Concepts for Estimating DCMs in Mplus 195
- 9.3 Preliminary Command Syntax 196
- 9.4 Parameterizing Latent Class Models for Categorical Data in Mplus 200
- 9.5 Syntax for Estimating the LCDM in Mplus 203
- 9.6 Syntax for Specifying Output Information 211
- 9.7 Running Mplus and Interpreting Output 213
- 9.8 Estimation of Core DCMs in Mplus 221
- 9.9 Advanced Topics for Mplus Estimation 224
- 9.10 Chapter Conclusion 231
### 10 • Respondent Parameter Estimation in DCMs
- 10.1 Principles of Estimation Relevant for Attribute Profile Estimation 232
- 10.2 Estimating Attribute Profiles 233
- 10.3 Extended Examples of Attribute Profile Estimation 235
- 10.4 EAP versus MAP Estimation 239
- 10.5 The Impact of Prior Attribute Distributions on Posterior Attribute Profile Estimation 241
- 10.6 Standard Errors for Attribute Profile Estimates 242
- 10.7 Attribute Profile Estimation in Mplus 243
- 10.8 Chapter Conclusion 247

### 11 • Item Parameter Estimation in DCMs
- 11.1 Conceptual Underpinnings for Estimating Item Parameters 250
- 11.2 Estimation of Item Parameters Using the E-M Algorithm 251
- 11.3 Estimation of Item Parameter Using MCMC 260
- 11.4 Chapter Conclusion 264

### 12 • Evaluating the Model Fit of DCMs
- 12.1 Basic Statistical Principles for Constructing Fit Statistics 266
- 12.2 Problems with General Goodness-of-Fit Statistics for DCMs 270
- 12.3 Practical Approaches for Determining Goodness-of-Fit for DCMs 271
- 12.4 An Example of Goodness-of-Fit Evaluation 275
- 12.5 Evaluating Relative Model Fit 277
- 12.6 Evaluating Person Fit 278
- 12.7 Chapter Conclusion 279

### 13 • Item Discrimination Indices for DCMs
- 13.1 Basic Concepts for Item Discrimination Indices 281
- 13.2 Item Discrimination Indices for DCMs 283
- 13.3 Information-Based Item Discrimination Indices for DCMs 294
- 13.4 Chapter Conclusion 304

### 14 • Accommodating Complex Sampling Designs in DCMs
- 14.1 Defining Complex Sampling Designs 306
- 14.2 Accommodating Complex Sampling Designs of Respondents in DCMs 307
- 14.3 Accommodating Complex Sampling Designs of Items in DCMs 310
- 14.4 Accommodating Additional Sources of Heterogeneity in DCMs 312
- 14.5 Chapter Conclusion 313

**Glossary**

**References**

**Author Index**

**Subject Index**

**About the Authors**

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For sample exercises, solutions, and data sets with associated Mplus code, see the book’s accompanying website at [projects.coe.uga.edu/dcm](http://projects.coe.uga.edu/dcm).