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For sample exercises, solutions, and data sets with associated *Mplus* code, see the book's accompanying website at [projects.coe.uga.edu/dcm](http://projects.coe.uga.edu/dcm).